XII Annual Seminar on Risk, Financial Stability and Banking

#### Implied volatility term structure and exchange rate predictability

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#### Main idea

# Can the currency implied volatility term structure (IVTS) predict exchange rate returns?

 Analysis from a time-series and cross-sectional perspective



### Main Result

Relationship between implied volatility term structure and returns DEPENDS ON THE MARKET

- Developed markets: negative relationship
- Emerging markets: positive relationship

# Motivation

- Exchange rate predictability is of interest to academics and market players, who can benefit from new currency investment strategies
- Different results have been computed in the literature, regarding the predictability of currency VRP (perhaps due to different option maturities)

#### Literature

- The term structure of option-implied volatilities has been studied for a long time
  - Poterba and Summers (1986)
  - Stein (1989)
  - Diz and Finucane (1993)
  - Heynen et al. (1994)
  - Xu and Taylor (1994)

#### Literature

- More recent papers attempt to predict the future shape of the volatility surface
  - Chalamandaris and Tsekrekos (2010, 2011)
  - Guo et al. (2014)
  - Buetow and Hendenrson (2016)
  - Luo and Zhang (2012)
  - Fassas (2012)



#### Literature

- Our paper is also related to the volatility risk premium (VRP) literature
  - Bollerslev et al. (2009, 2014)
  - Ornelas (2017)
  - Londoño and Zhou (2017)
  - Della Corte et al. (2016)
  - Ornelas and Mauad (2017)



# What we do

- We build IVTS using three types of IV: ATM and 10delta IV for the left and right tails (indirect quote)
- For each type, we use options with ten different maturity periods, ranging from one week to ten years
- We calculate each day the slope of the IVTS for these three types of IV, and for each of the 18 currencies in our sample (10 developed and 8 emerging markets)



# Sample

- We obtain IV from over-the-counter (OTC) exchange rate options (estimates from JP Morgan data query application)
- Daily data from 2002 to 2016
- The following currencies against the US dollar:
- G10 currencies:
  - AUD, EUR, GBP, NZD, CAD, CHF, DKK, JPY, NOK and SEK
- Emerging market currencies:
  - BRL, CLP, CZK, HUF, MXN, PLN, THB and ZAR.

# Implied volatility term structure

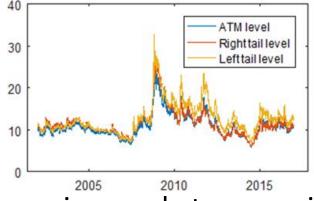
$$IV_{i,j,t} = \alpha_{i,t} + \beta_{i,t} * Mat_j + \varepsilon_{i,t}$$

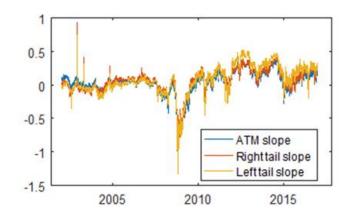
- Where
- $IV_{i,j,t}$  is the implied volatility for currency *i*, maturity  $Mat_j$  on date *t*
- $Mat_j$  is the  $j^{th}$  maturity in years
- α<sub>i,t</sub> is estimated the average level of the volatility term structure for currency *i* on date *t*
- $\beta_{i,t}$  is estimated the slope of the volatility term structure for currency *i* on date *t*
- We use the three aforementioned types of IV in this regression: ATM, right and left tail with delta 10



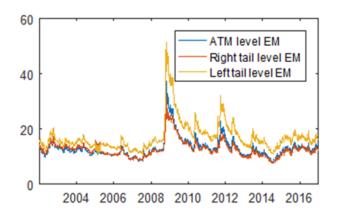
# Implied volatility term structure

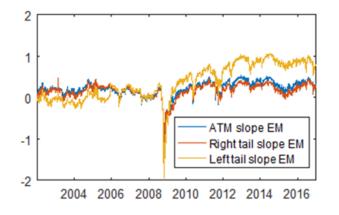
• G10 currencies





• Emerging market currencies





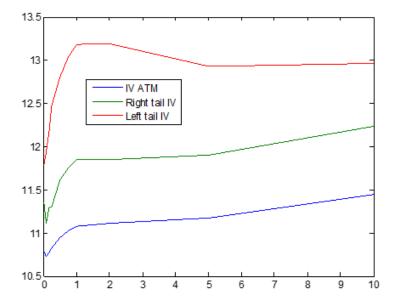
#### Average level and slope for each IV

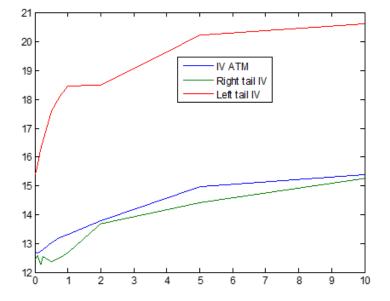
		Implie	d Volatilit	y Level	Implie			
Currencies		АТМ	Left tail delta 10	Right tail delta 10	АТМ	Left tail delta 10	Right tail delta 10	Realized Volatility
					Panel A			
	AUD	11,05	13,66	10,86	0,02	0,14	0,01	11,78
	CAD	8,69	10,01	9,01	0,05	0,10	0,05	8,54
	CHF	9,83	10,83	10,86	0,01	0,00	0,05	10,96
	DKK	9,58	11,09	9,99	0,03	0,05	0,03	9,18
Developed	EUR	9,55	11,00	10,01	0,03	0,06	0,03	9,22
economies	GBP	8,74	10,31	9,03	0,10	0,13	0,10	8,40
	JPY	9,72	9,89	12,18	0,08	0,05	0,32	9,44
	NOK	11,28	12,90	11,58	0,00	0,02	-0,01	11,52
	NZD	12,09	14,79	11,91	0,01	0, 12	0,00	12,28
	SEK	11,18	12,79	11,50	0,01	0,03	0,00	11,30
					Panel B			
	BRL	15,21	20,81	14,09	0,38	0,44	0,37	15,70
	CLP	11,02	14,73	10,76	0,22	0,35	0,14	9,38
	CZK	11,23	13,44	11,49	0,03	0,12	-0,03	11,54
Emerging	HUF	13,40	17,69	13,06	0,14	0,29	0,09	13,69
markets	MXN	10,76	14,33	10,08	0,28	0,43	0,33	9,85
	PLN	12,93	16,36	12,90	0,04	0, 16	-0,02	12,93
	THB	6,29	8,16	6,67	0,25	0,39	0,21	4,62
	ZAR	16,23	21,86	15,44	0,19	0,53	0,09	16,68

# Term Structure of Implied Volatility

• G10 currencies

• Emerging market currencies





### **Time-series predictability**

$$Ret_{i,h,t} = \alpha + \gamma_1 * \beta_{i,t} + \gamma_2 * Ret_{i,h,t-h}$$

- Where
- *Ret*<sub>*i*,*h*,*t*</sub> is the return for each holding period *h* (three or six months), for each currency *i*, starting at time *t*;
- $\beta_{i,t}$  is the coefficient previously estimated for each currency, each day.
- Results are shown in the next slide

#### Exchange rate return regression results

Dependent Variable (Currency Returns)		ATM		Left tail		Right tail			
		Coefficients							
		3 Mo	6 Mo	3 Mo	6 Mo	3 Mo	6 Mo		
				Pa	nel A				
	AUD	-6.83**	-14.22***	-5.61***	-11.87***	-7.65***	-15.99***		
	EUR	-2.80	-5.52	-2.98	-5.91	-4.66**	-9.51*		
	GBP	1.03	0.42	-0.04	-1.33	-0.92	-4.22		
	NZD	-4.78	-13.38***	-4.16*	-10.15***	-6.03	-16.23***		
Developed	CAD	-5.62*	-13.32**	-4.70**	-11.54***	-5.76*	-13.90***		
economies	CHF	-0.44	-2.29	-0.72	-2.94	-1.64	-4.39		
	DKK	-3.57	-6.54	-4.45**	-8.39*	-5.72***	-10.70**		
	JPY	-2.65	-6.10	-2.47	-5.83	-2.52	-5.71*		
	NOK	-4.52	-8.42	-5.09**	-9.65**	-6.88***	-13.04**		
	SEK	-5.18*	-8.99	-5.21**	-9.61**	-7.48***	-13.73***		
				Ра	nel B				
	BRL	3.99	3.40	3.14***	5.88*	1.86	-0.31		
	CLP	-2.19	-6.49	1.64	2.33	-2.07	-7.93		
	CZK	3.29	5.24	2.82	5.91**	4.04	6.08		
Emerging	HUF	2.75	5.30	1.86	4.02*	3.12	6.53		
markets	MXN	-1.46	2.12	0.04	3.24	-2.19	-3.39		
	PLN	1.02	2.90	1.15	3.14	2.77	5.33		
	THB	1.64	2.46	1.97**	4.09***	1.46	1.89		
	ZAR	7.17***	16.36***	3.44***	7.38***	8.22***	18.60***		

#### **Economic Intuition**

- Volatility risk premium is important for emerging markets, but not for developed
- Developed: negative (positive) slope would mean physical volatility above (below) long-term equilibrium, and future volatility would decrease (increase)
- EM: high (low) slope would mean a higher (lower) risk premia. This means currencies are under (over) valued, and then should recover (go down) in the future

# **Cross-Section predictability**

- We build long-short (cash neutral) portfolios based on the slopes of the volatility term structure
- Developed countries: short on top 20% slopes and long on bottom 20%
- Emerging markets: long on top 25% slopes and short on 25% bottom
- We form these portfolios on a daily basis and hold them for three months (63 overlapping business days) – each has a weight of 1/63.

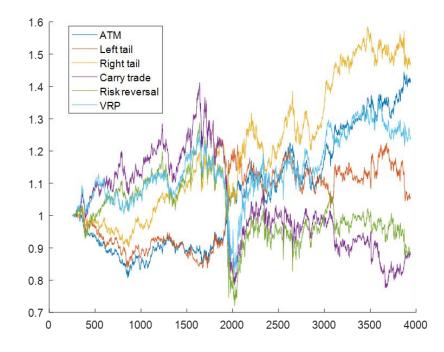


# **Cross-Section predictability**

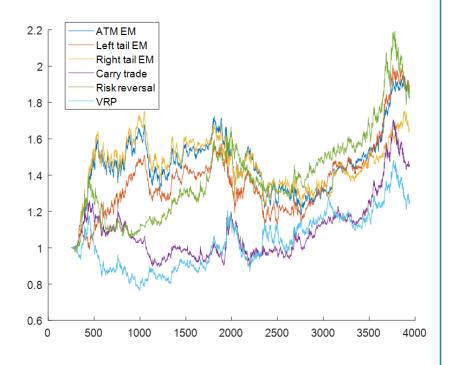
- To benchmark this exchange rate investment strategy, we use three other types of strategy:
  - Carry trade (based on interest rates)
  - Risk-reversal average level for the 10-delta
  - One-year VRP

#### Portfolio comparison with benchmark strategies

• G10 currencies



Emerging Markets



# Portfolio return statistics- Currency

		Currency Returns								
	Types of portfolios	Mean (Geo) Returns	Mean (Ari) Returns	Volatility	Skewness	Kurtosis	Sharpe Ratio (Geo)	Sharpe Ratio (Ari)		
				Panel A - I	Developed	markets				
	ATM Slope	2,39%	2,33%	7,00%	0,095	6,4	0,34	0,33		
	Left Tail Slope	0,37%	0,38%	7,63%	1,090	17,5	0,05	0,05		
Developed	Right Tail Slope	2,67%	2,80%	8,36%	-0,481	14,7	0,32	0,33		
economies	Carry Trade	-0,88%	0,13%	12,49%	-0,930	19,2	-0,07	0,01		
	Risk-Reversal	-0,86%	0,22%	12,63%	-0,670	17,4	-0,07	0,02		
	VRP	1,46%	2,02%	11,20%	-0,456	15,4	0,13	0,18		
				Panel B - I	Emerging N	<b>Aarkets</b>				
	ATM Slope	4,31%	4,67%	10,74%	-0,026	5,8	0,40	0,43		
	Left Tail Slope	4,48%	4,59%	9,79%	-0,023	5,6	0,46	0,47		
Emerging	Right Tail Slope	3,52%	4,00%	10,96%	-0,086	6,7	0,32	0,36		
markets	Carry Trade	2,62%	3,05%	11,42%	0,251	9,0	0,23	0,27		
	Risk-Reversal	4,38%	4,56%	11,50%	0,377	7,6	0,38	0,40		
	VRP	1,62%	2,19%	12,97%	0,507	6,9	0,13	0,17		

# Portfolio return statistics - Total

	Total Return							
	- Types of portfolios	Mean (Geo) Returns	Mean (Ari) Returns	Volatility	Skewness	Kurtosis	Sharpe Ratio (Geo)	Sharpe Ratio (Ari)
	_		Pane	l A - Devel	loped mark	ets		
	ATM Slope	2,34%	2,29%	7,00%	0,098	6,3	0,33	0,33
	Left Tail Slope	-0,69%	-0,61%	7,63%	1,080	17,4	-0,09	-0,08
Developed	Right Tail Slope	4,16%	4,18%	8,36%	-0,469	14,7	0,50	0,50
economies	Carry Trade	3,41%	4,14%	12,49%	-0,923	19,2	0,27	0,33
	<b>Risk-Reversal</b>	2,68%	3,53%	12,63%	-0,659	17,4	0,21	0,28
	VRP	3,51%	3,93%	11,20%	-0,444	15,4	0,31	0,35
	_		Par	el B - Eme	erging Marl	kets		
	ATM Slope	7,29%	7,42%	10,74%	-0,027	5,8	0,68	0,69
	Left Tail Slope	6,68%	6,64%	9,79%	-0,040	5,6	0,68	0,68
Emerging	Right Tail Slope	6,35%	6,61%	10,96%	-0,086	6,7	0,58	0,60
markets	Carry Trade	13,42%	13,07%	11,42%	0,267	9,0	1,18	1,15
	<b>Risk-Reversal</b>	12,08%	11,71%	11,50%	0,389	7,6	1,05	1,02
	VRP	8,03%	8,17%	12,97%	0,517	6,9	0,62	0,63

#### **Correlation matrices**

		ATM Slope	Left Tail Slope	Right Tail Slope	Carry Trade	Risk- Reversal	VRP			
			Pa	nelA - Deve	loped ma	rkets				
	ATM Slope		59%	67%	18%	22%	41%			
	Left Tail Slope	59%		18%	-35%	-25%	-10%			
Developed	Right Tail Slope	67%	18%		56%	62%	67%			
economies	Carry Trade	18%	-35%	56%		91%	74%			
	Risk-Reversal	22%	-25%	62%	91%		84%			
	VRP	41%	-10%	67%	74%	84%				
		Panel B - Emerging Markets								
	ATM Slope		75%	92%	13%	22%	-26%			
	Left Tail Slope	75%		61%	6%	14%	-25%			
<b>.</b> .	Right Tail Slope	92%	61%		9%	16%	-31%			
Emerging markets	Model-Free Slope	97%	75%	90%	17%	26%	-21%			
mai Kets	Carry Trade	13%	6%	9%		78%	70%			
	Risk-Reversal	22%	14%	16%	78%		72%			
	VRP	-26%	-25%	-31%	70%	72%				

# Final remarks

- This paper provides new empirical evidence that the slopes of currency IVTS have predictive power for the exchange rates behavior from both cross-section and time-series perspectives
- Intriguingly, the direction of the prediction is not the same for developed and emerging markets.
- The proposed strategy performs better than common currency based on the Sharpe ratio, considering currency returns